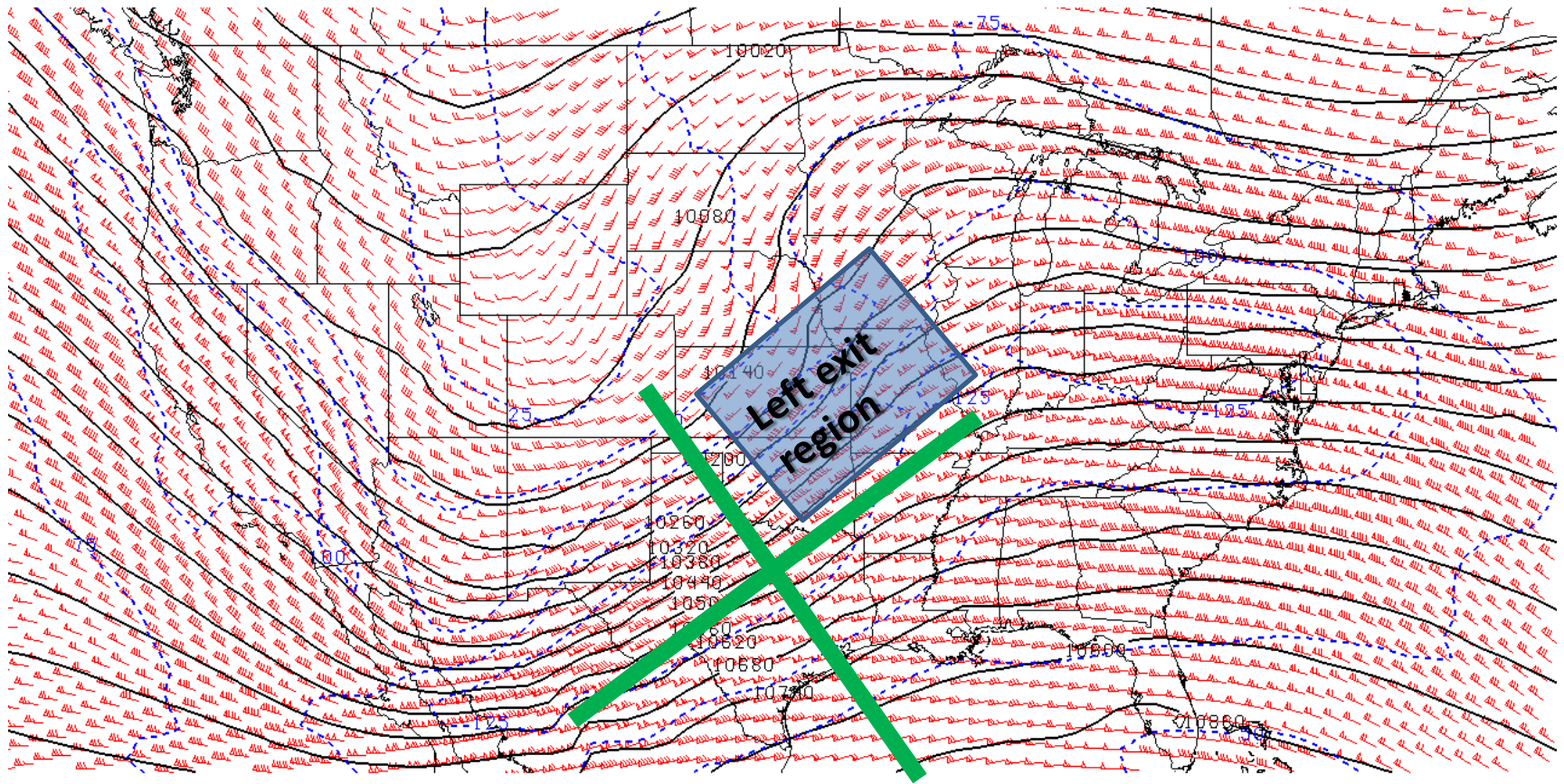


ATMO 574  
Homework #2 Key  
100 points Total

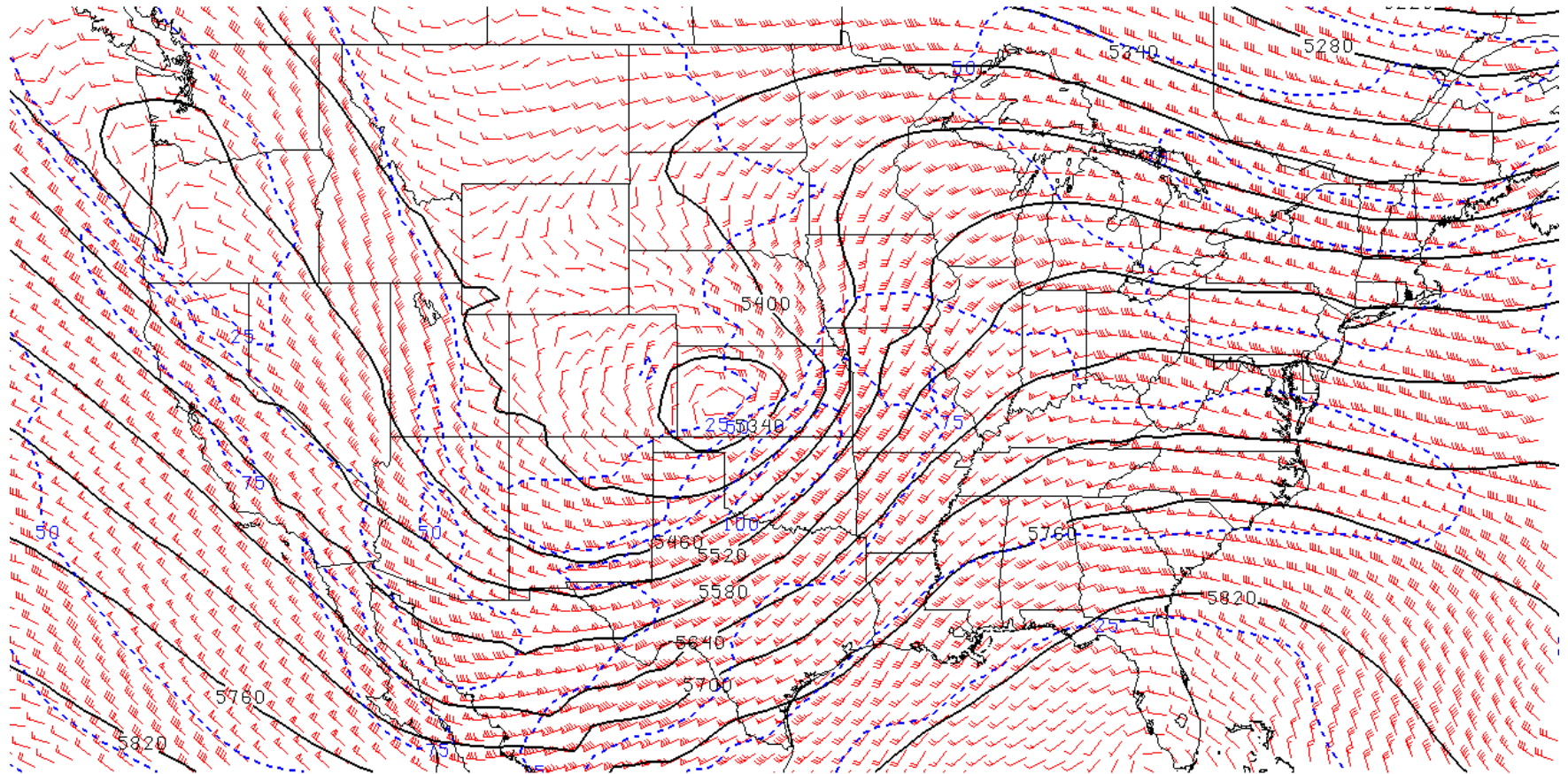
# Part 1: Upper-air map plotting and discussion

25 points

# 250-mb heights (m) and isotachs (kt)



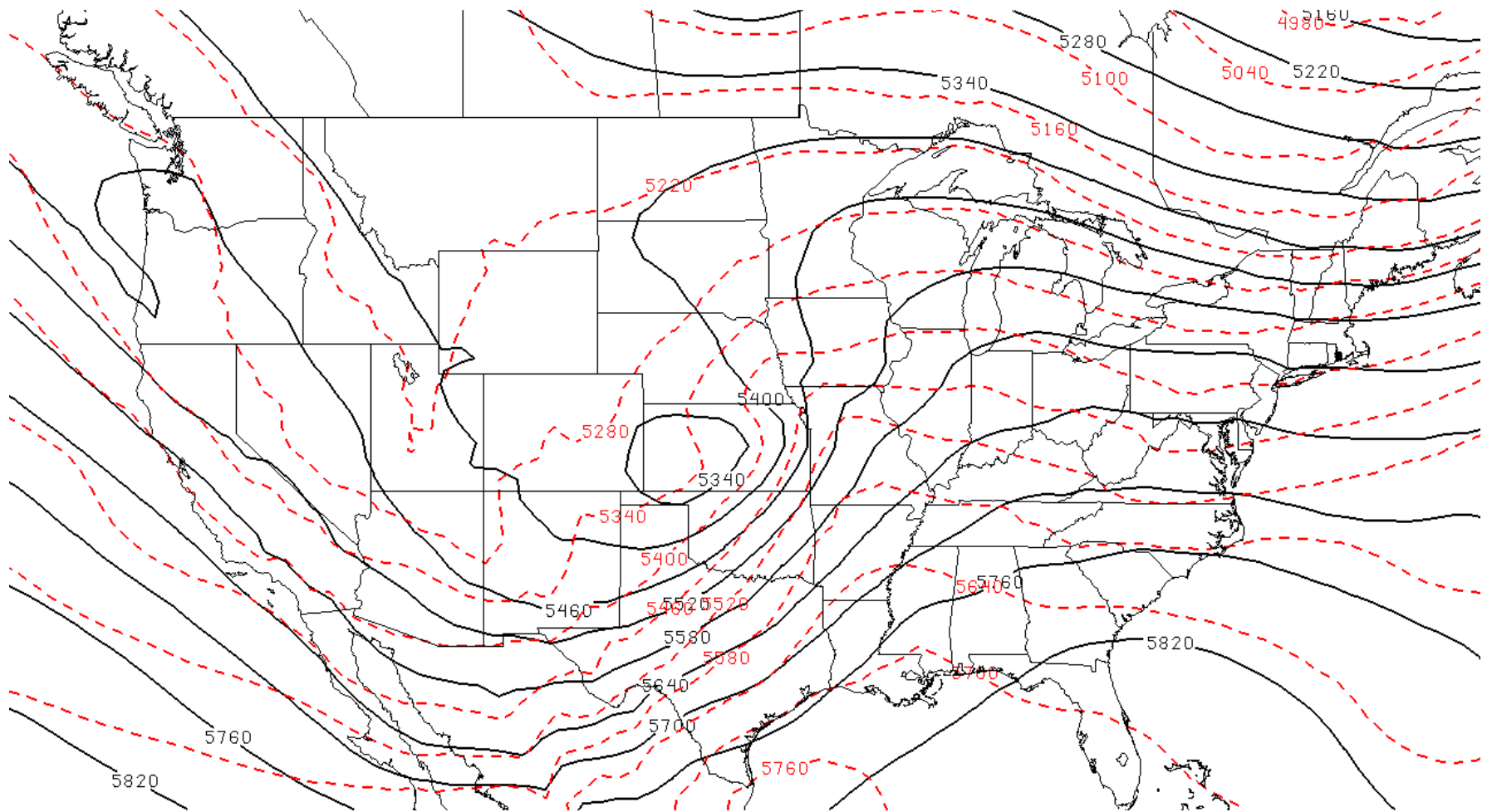
# 500-mb heights (m) and isotachs (kt)



17 JAN 2025 0000 UTC NCEP/NCAR

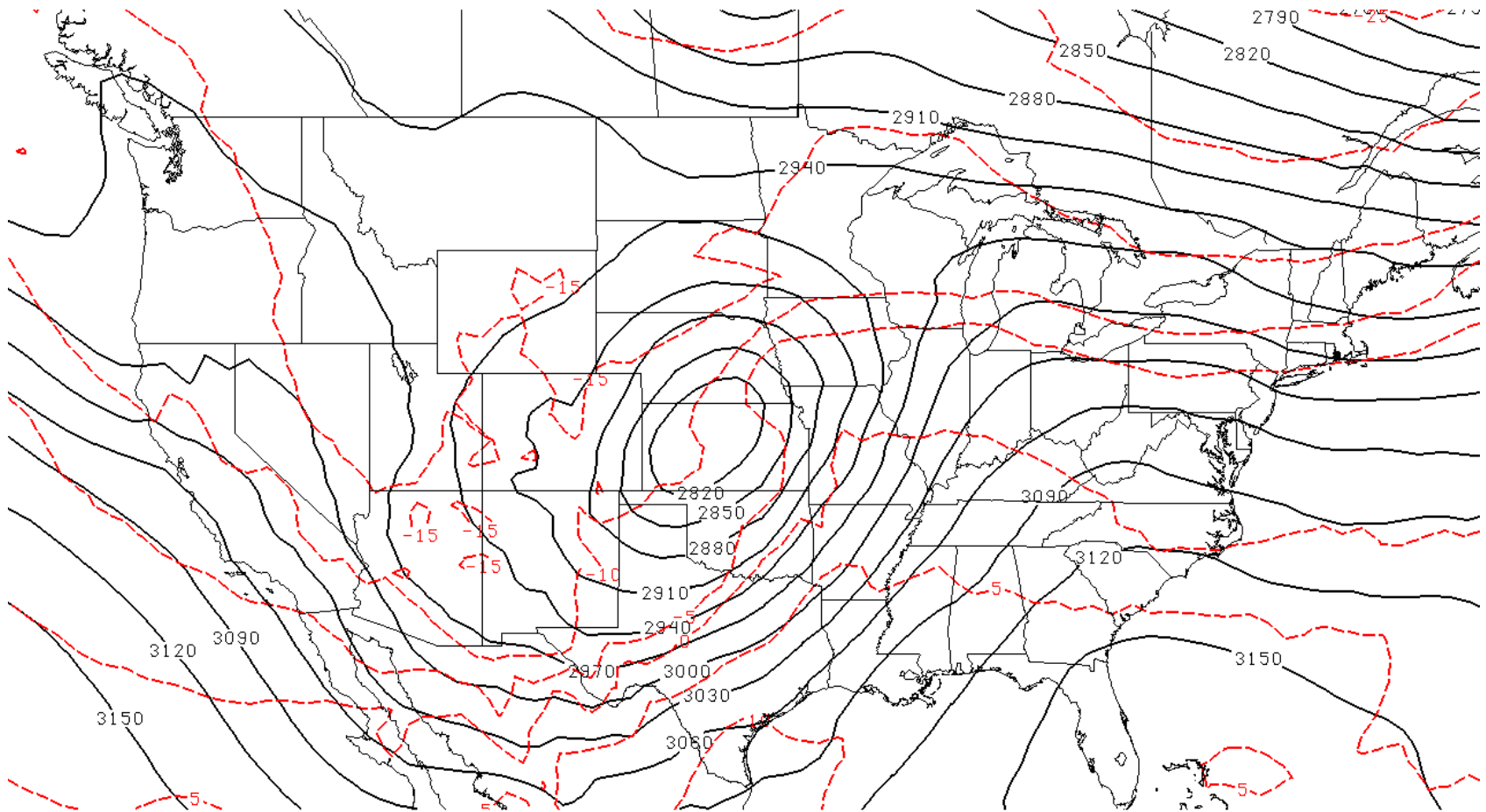
# 500-mb heights (m)

## 1000 to 500-mb thickness (m)



1701027020270000V800 : 500055MBH6H0FHGHT

# 700-mb heights (m) and temperature ( $^{\circ}\text{C}$ )



170102/1200V000 700 MB R6MF

## **Part 1: Summary points for discussion**

Consistent with what we concluded earlier for HW #1, the upper-air analysis confirms that the mid-latitude cyclone is in a fully mature to advanced occluded stage of development. Still some baroclinicity evident by presence of temperature advection and (slight) westward tilt of the low.

The upper-air trough tends to have a negative tilt, meaning it is tilting against the mean shear and able to import vorticity to intensify the strength of the eddy. This is characteristic of a very mature, strong mid-latitude cyclone.

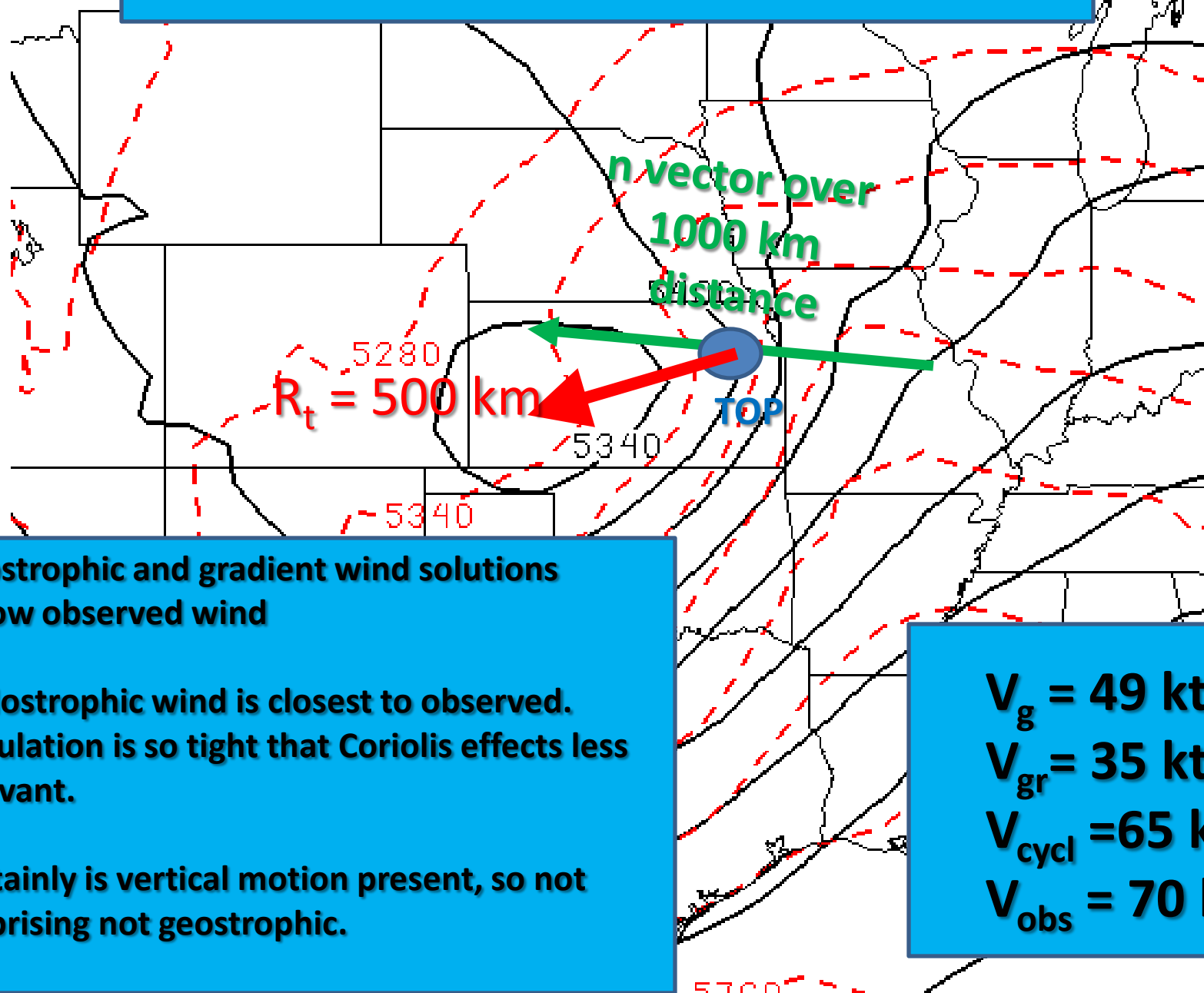
There is evidence of a jet streak in the 250-mb analysis centered in central Texas with winds in excess of 125 kts. The location of the surface low and all the significant weather that merited watch, warning criteria (e.g. heavy snow in Nebraska) are located in the left exit region of the jet streak. This is favorable for cyclone development and weather because upward vertical motion is favored there in a thermally indirect transverse circulation.

# Part 2: Hand calculations of balanced winds, thermal wind, and kinematic properties

25 points



## Balanced wind solutions sample calculation



**Geostrophic and gradient wind solutions  
below observed wind**

Cyclostrophic wind is closest to observed.  
Circulation is so tight that Coriolis effects less  
relevant.

Certainly is vertical motion present, so not  
surprising not geostrophic.

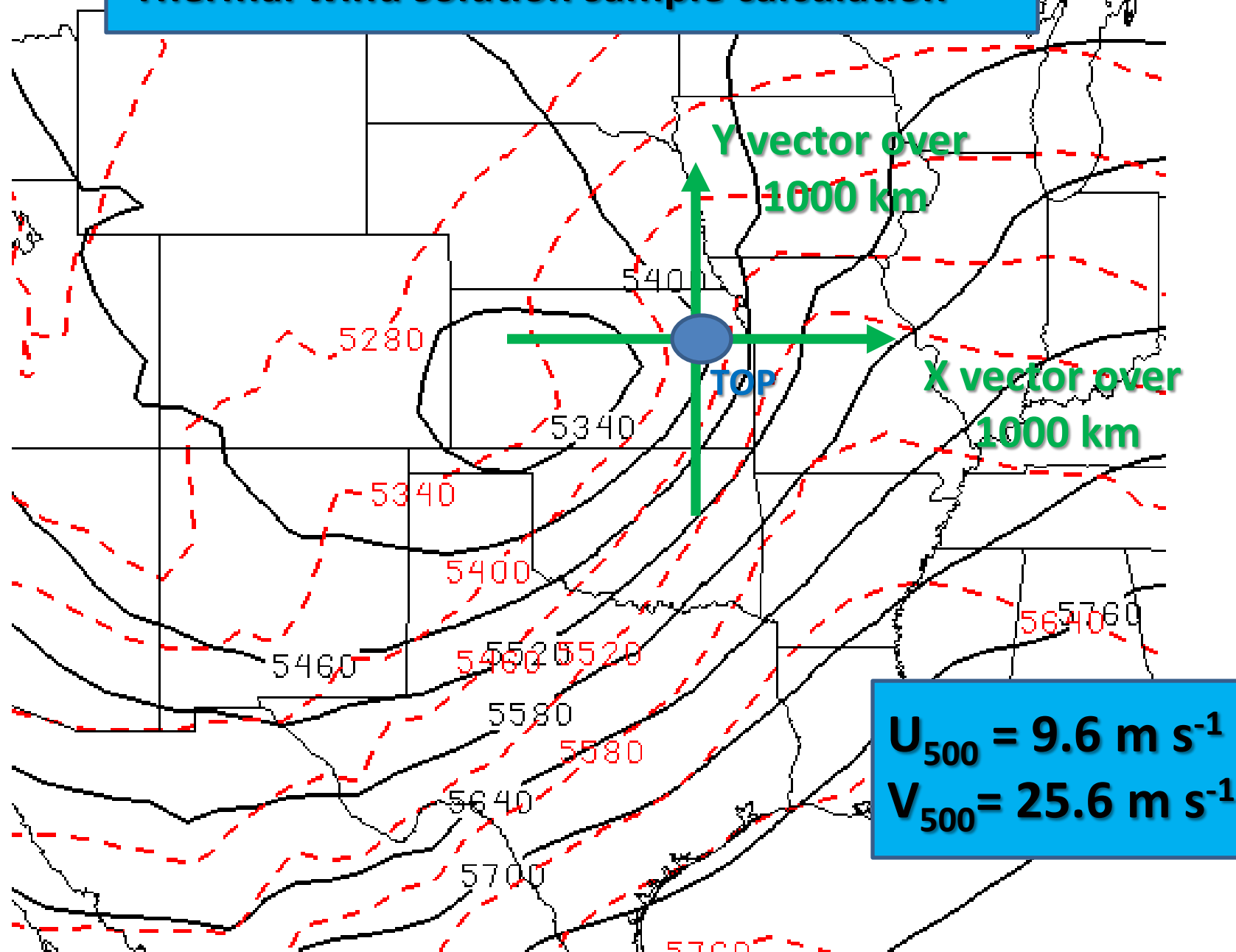
$$V_g = 49 \text{ kts}$$

$$V_{gr} = 35 \text{ kts}$$

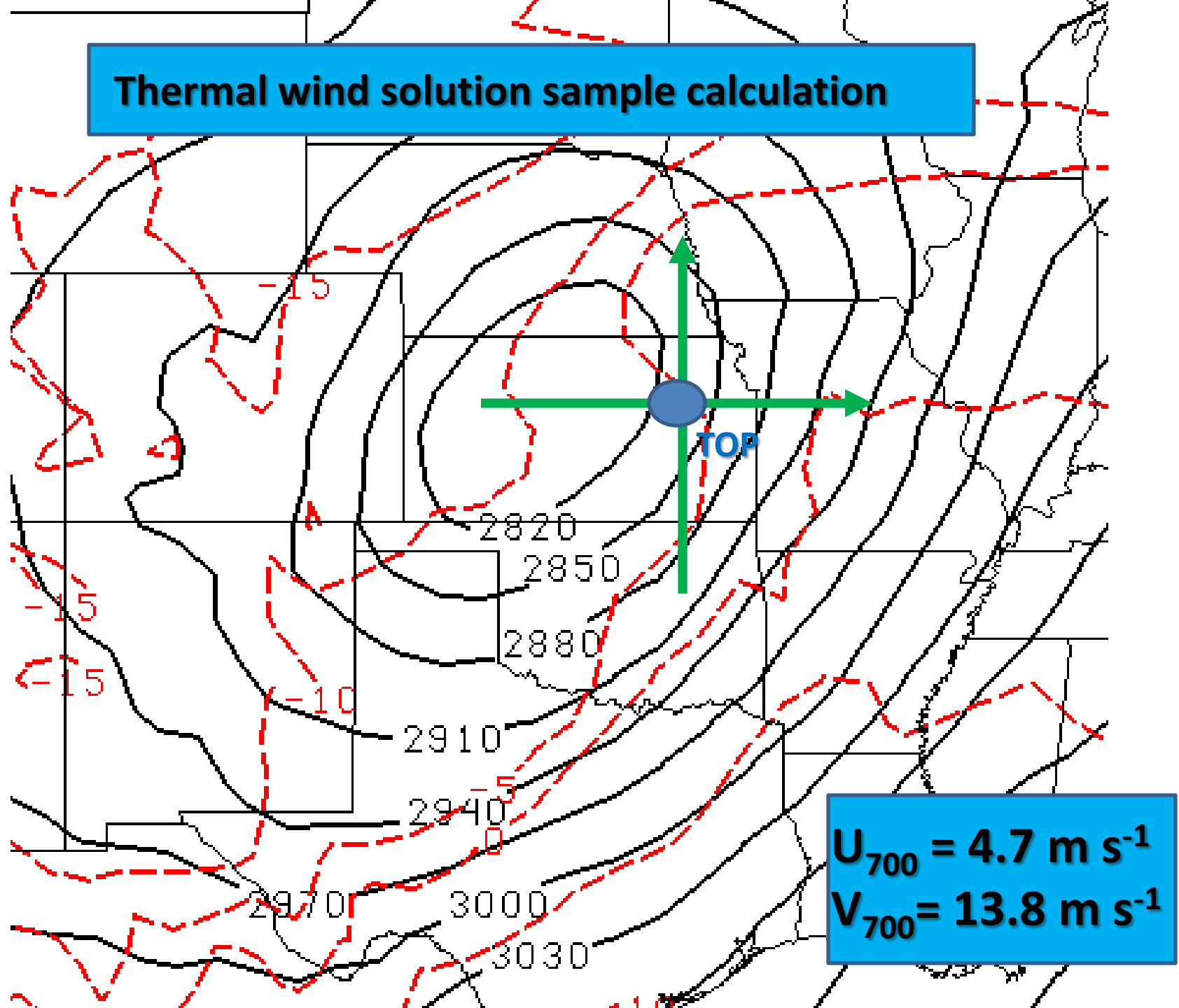
$$V_{cycl} = 65 \text{ kts}$$

$$V_{obs} = 70 \text{ kts}$$

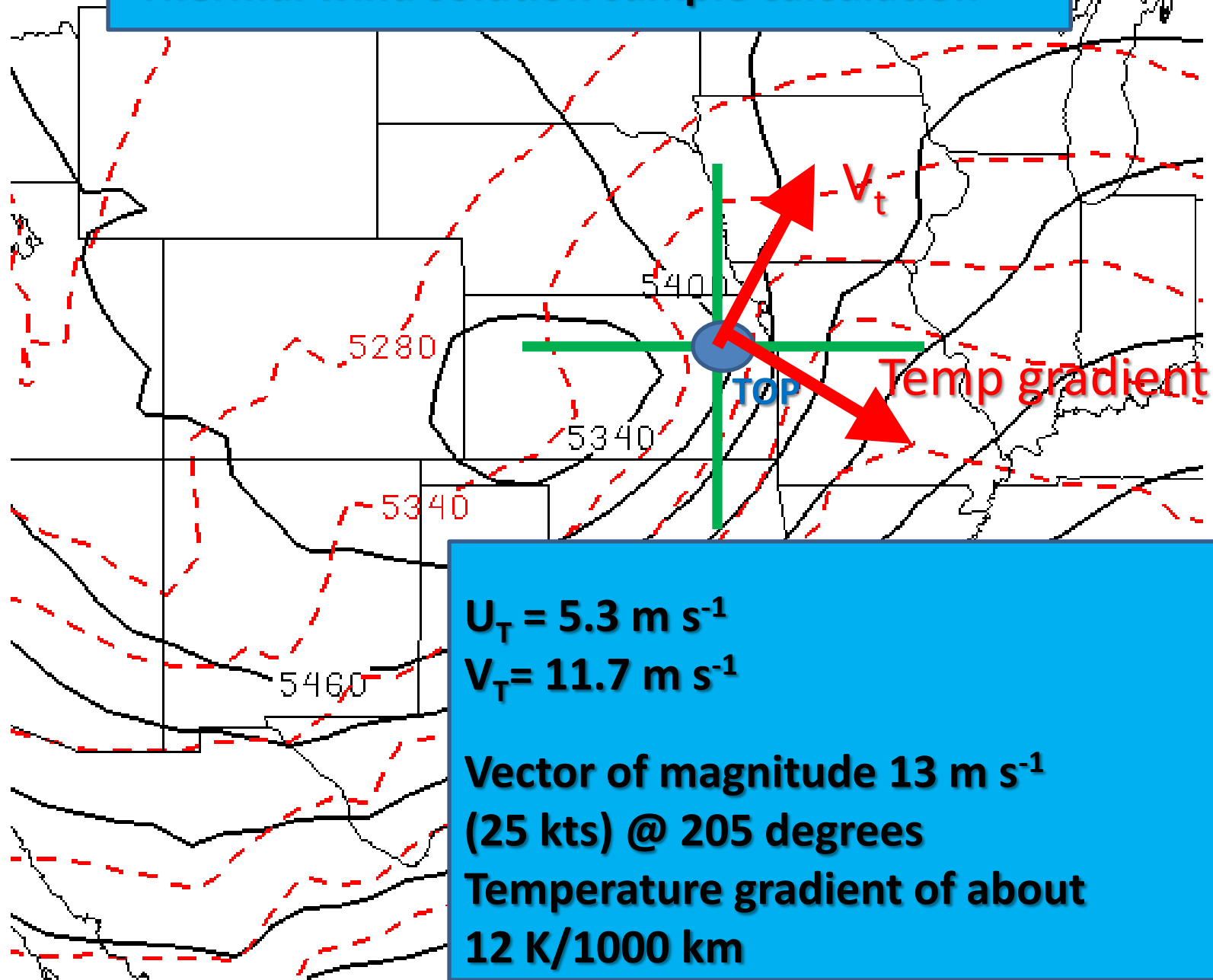
## Thermal wind solution sample calculation



## Thermal wind solution sample calculation



## Thermal wind solution sample calculation



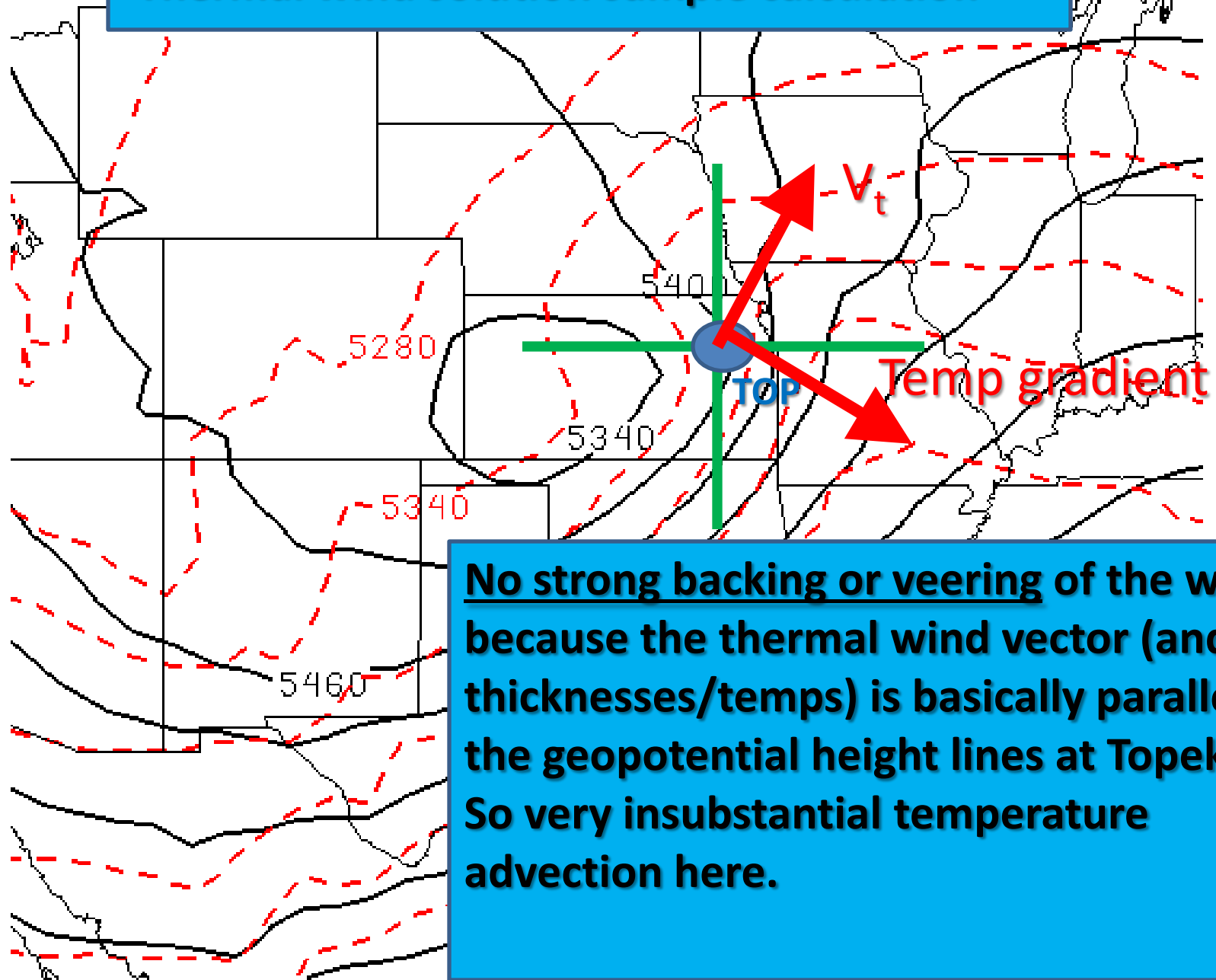
$$U_T = 5.3 \text{ m s}^{-1}$$

$$V_T = 11.7 \text{ m s}^{-1}$$

Vector of magnitude  $13 \text{ m s}^{-1}$   
(25 kts) @ 205 degrees

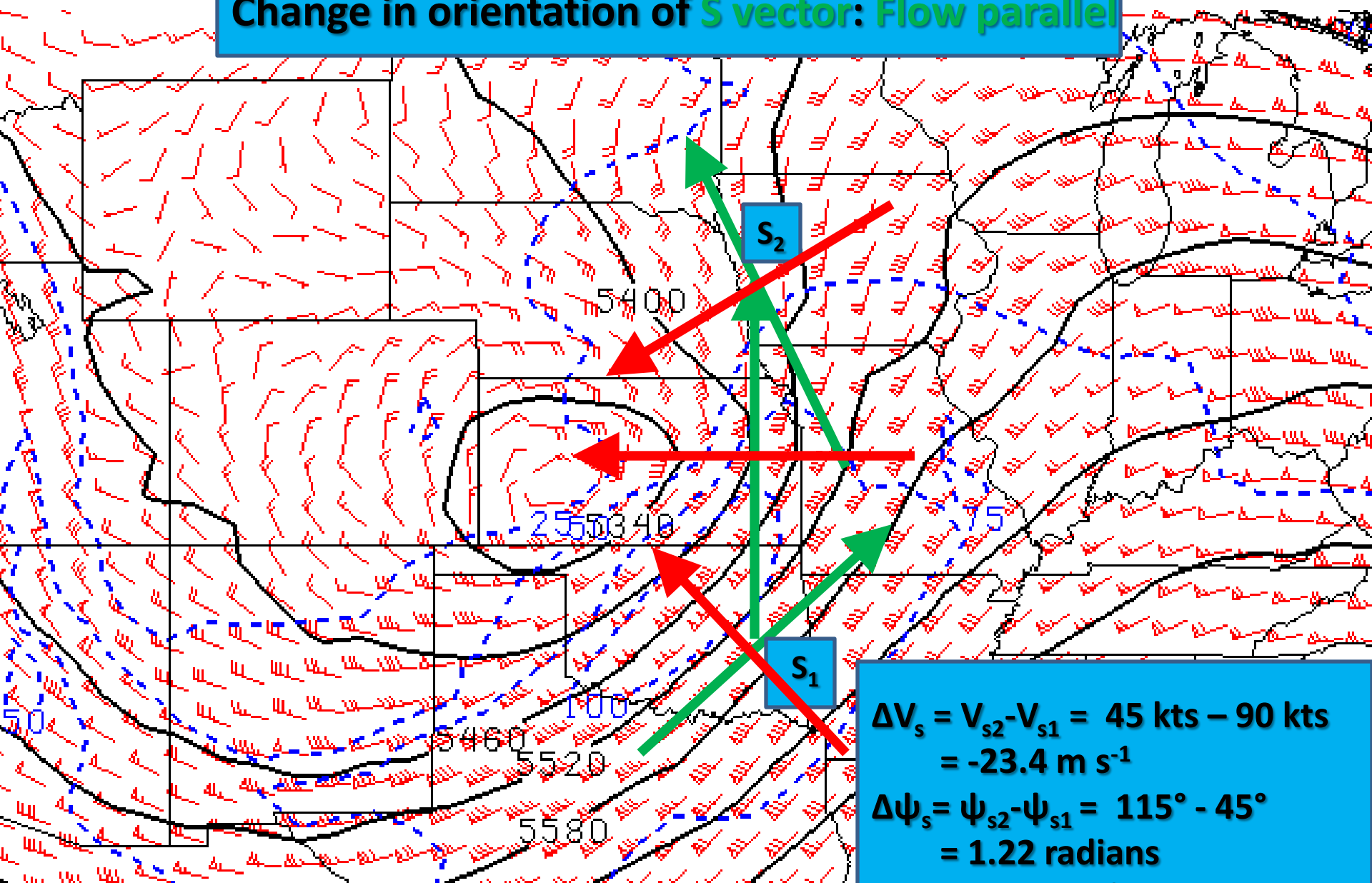
Temperature gradient of about  
 $12 \text{ K/1000 km}$

## Thermal wind solution sample calculation



**No strong backing or veering of the wind**  
because the thermal wind vector (and  
thicknesses/temps) is basically parallel to  
the geopotential height lines at Topeka.  
So very insubstantial temperature  
advection here.

## Change in orientation of **S** vector: Flow parallel

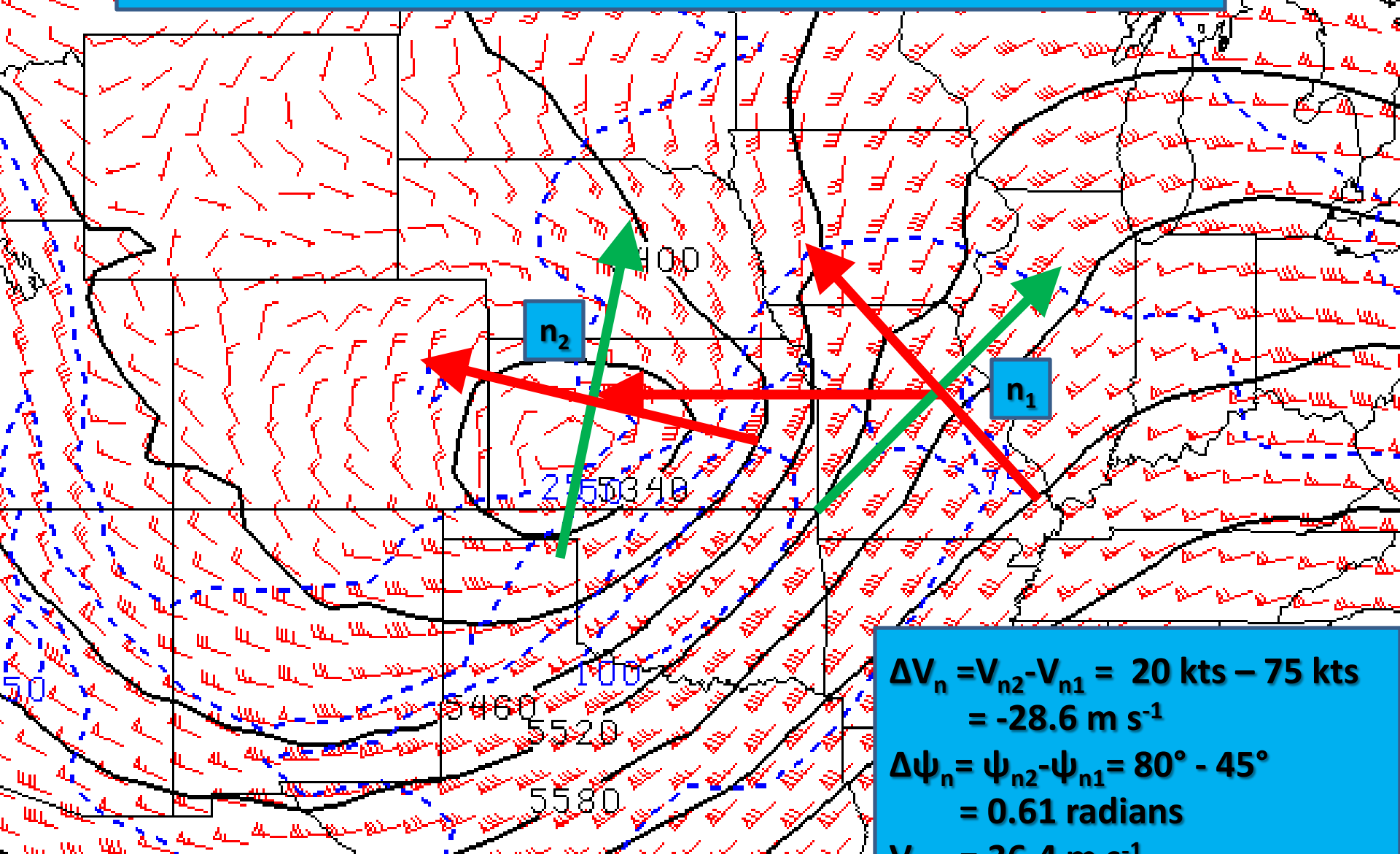


$$\Delta \mathbf{V}_s = \mathbf{V}_{s2} - \mathbf{V}_{s1} = 45 \text{ kts} - 90 \text{ kts} \\ = -23.4 \text{ m s}^{-1}$$

$$\Delta \psi_s = \psi_{s2} - \psi_{s1} = 115^\circ - 45^\circ \\ = 1.22 \text{ radians}$$

$$\mathbf{V}_{\text{Top}} = 36.4 \text{ m s}^{-1}$$

## Change in orientation of **n** vector: flow perpendicular



$$\Delta V_n = V_{n2} - V_{n1} = 20 \text{ kts} - 75 \text{ kts} \\ = -28.6 \text{ m s}^{-1}$$

$$\Delta \psi_n = \psi_{n2} - \psi_{n1} = 80^\circ - 45^\circ \\ = 0.61 \text{ radians}$$

$$V_{\text{Top}} = 36.4 \text{ m s}^{-1}$$

## Sample results for kinematic quantities ( $10^{-5} \text{ s}^{-1}$ )

Shear: 2.86

Curvature: 4.45

Vorticity: 7.31

**Flow has positive curvature which is greatest contributor to positive (cyclonic vorticity)**

Diffluence: 2.27

Stretching: -2.34

Divergence: -0.16

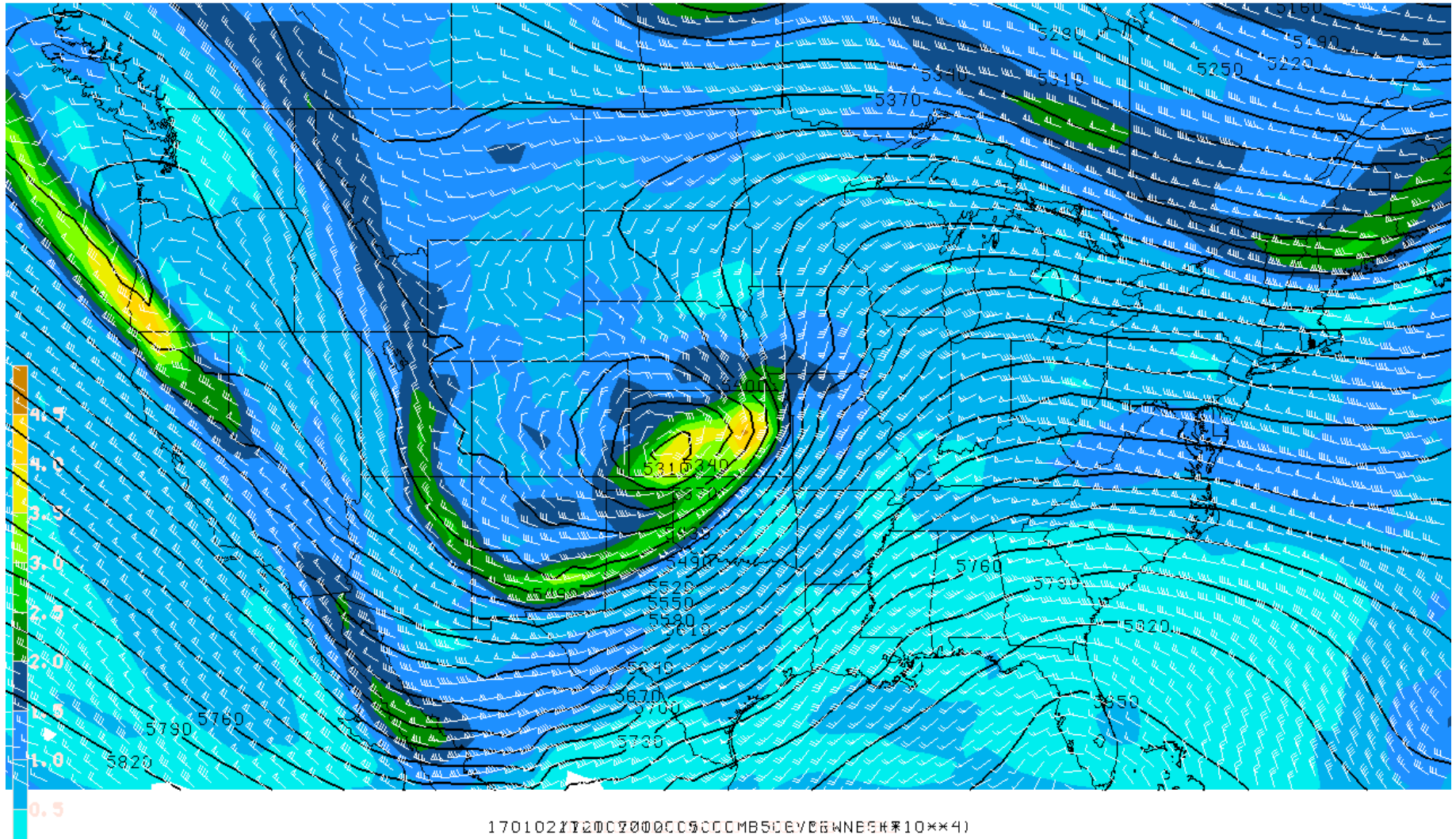
**Flow is diffluent but negative stretching, so divergence is less in magnitude than vorticity.**



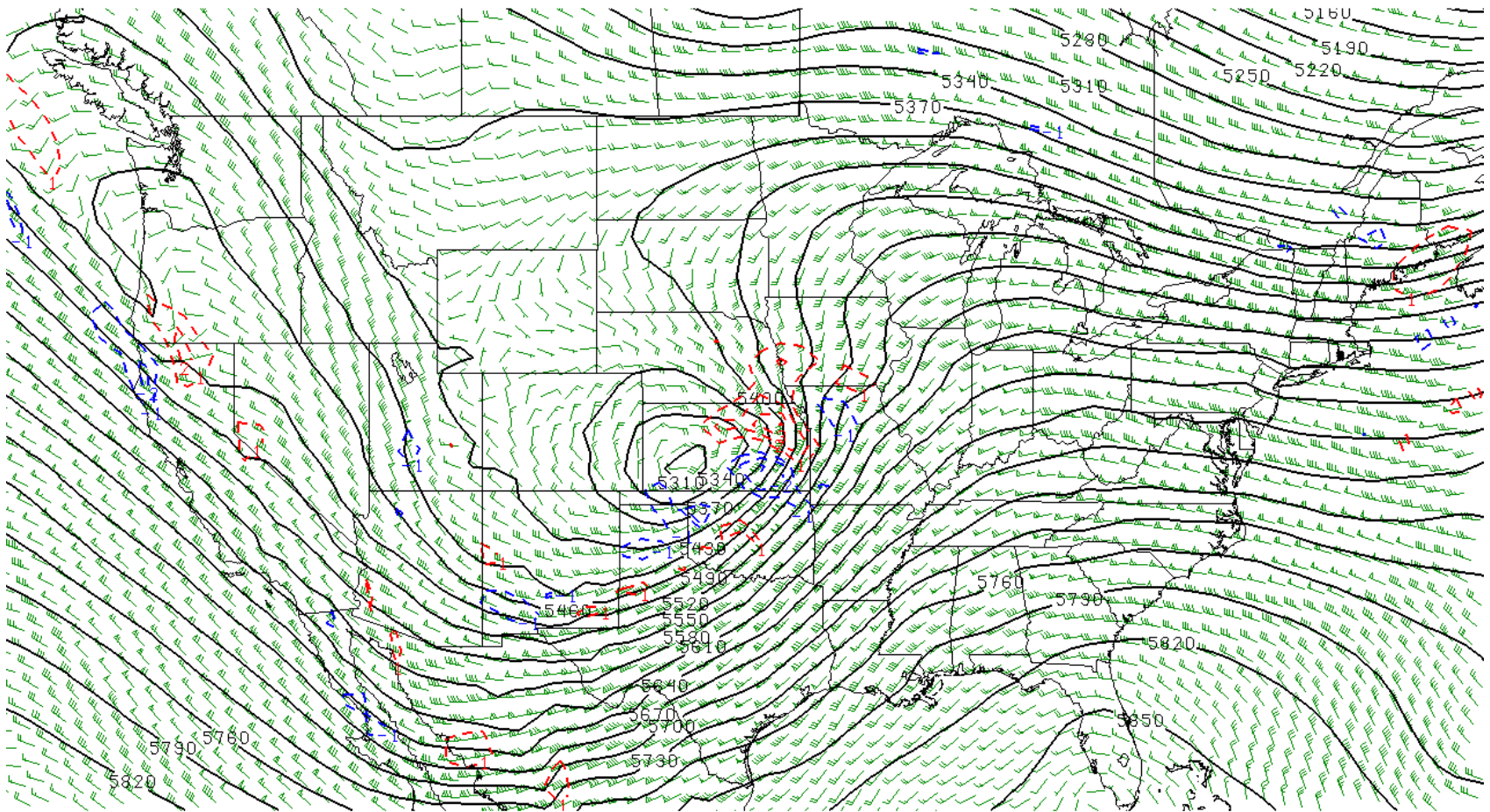
# Part 3: Analysis of terms in QG-omega equation from GEMPAK maps

25 points

# 500-mb Vorticity



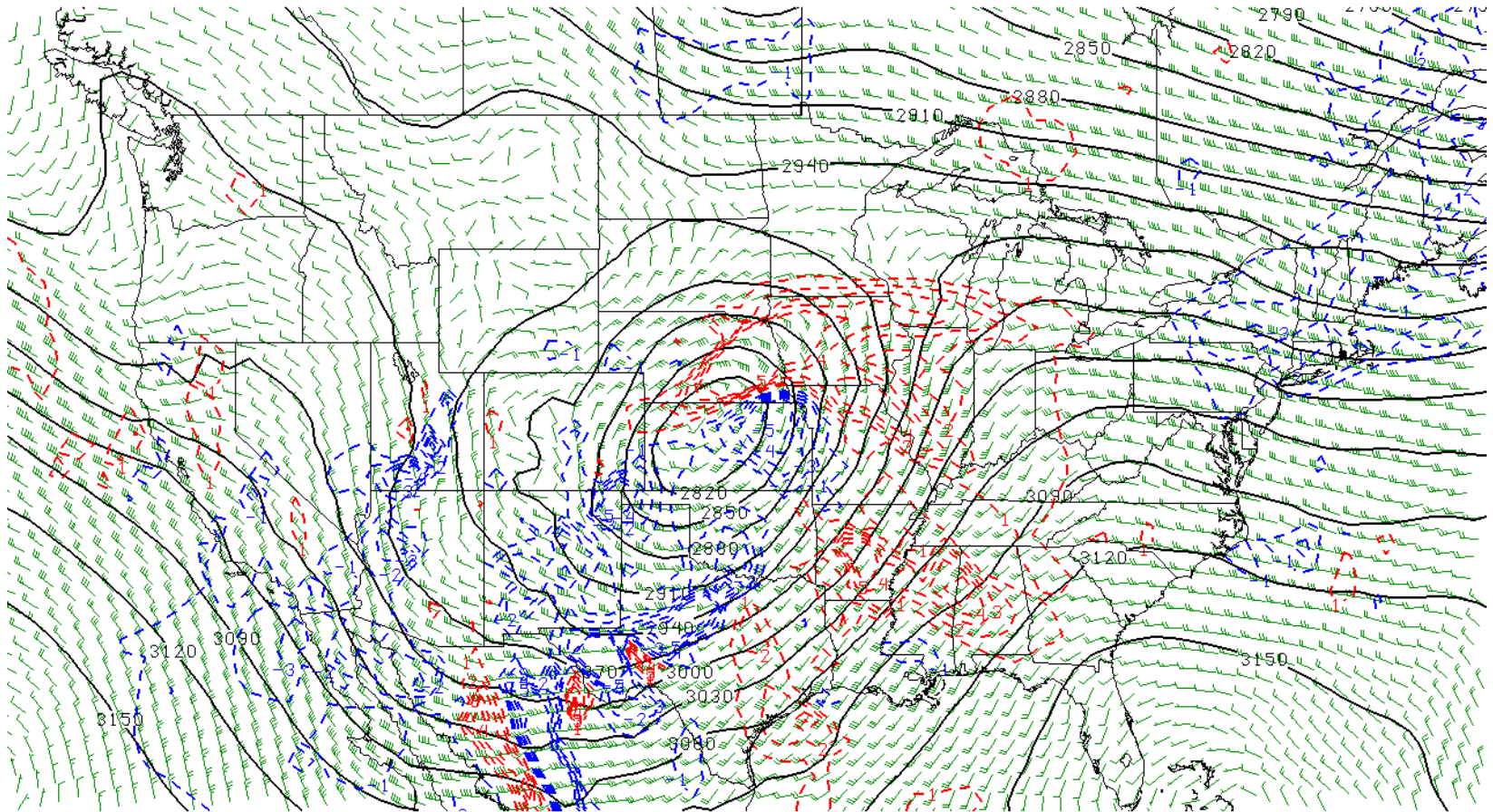
# 500-mb Vorticity Advection



170102/1200Y00012000000 BD00MBRUBBT (\*10\*\*8)



# 700-mb Temperature Advection



170102/1200Y000120000000 000TMBKUBBT (\*10\*\*4)

### **Part 3: Summary points for discussion**

Strongest PVA to the north and east of the upper-level low in northeast Kansas, southwest Nebraska. Strongest NVA just south of that.

Strongest WAA advection in the vicinity of where heaviest precipitation is observed in Nebraska.

Where WAA, PVA coincide in southeastern Nebraska corresponds to where most significant weather is occurring in relation to this mid-latitude cyclone. Recall the “worst” weather occurring at Offutt AFB (thundersnow)

Coinciding CAA, NVA correspond to the dry slot area wrapping around the surface low.

**Overall, the QG approach works well here in terms of correspondence of significant weather and synoptic scale upward vertical motion.**

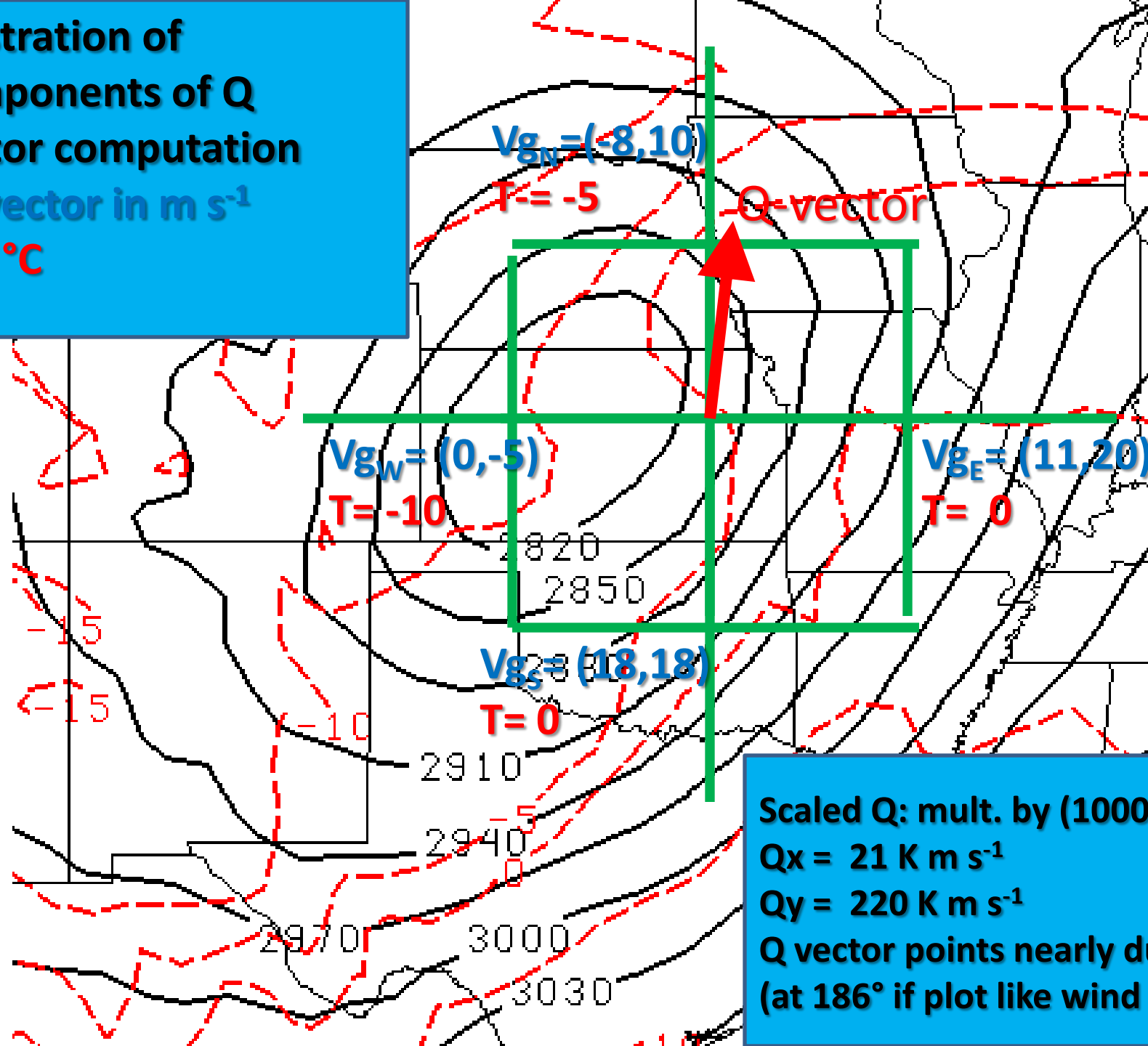
## Part 4: Analysis of Q-vector

25 points

# Illustration of components of Q vector computation

Vg vector in  $\text{m s}^{-1}$

T in  $^{\circ}\text{C}$



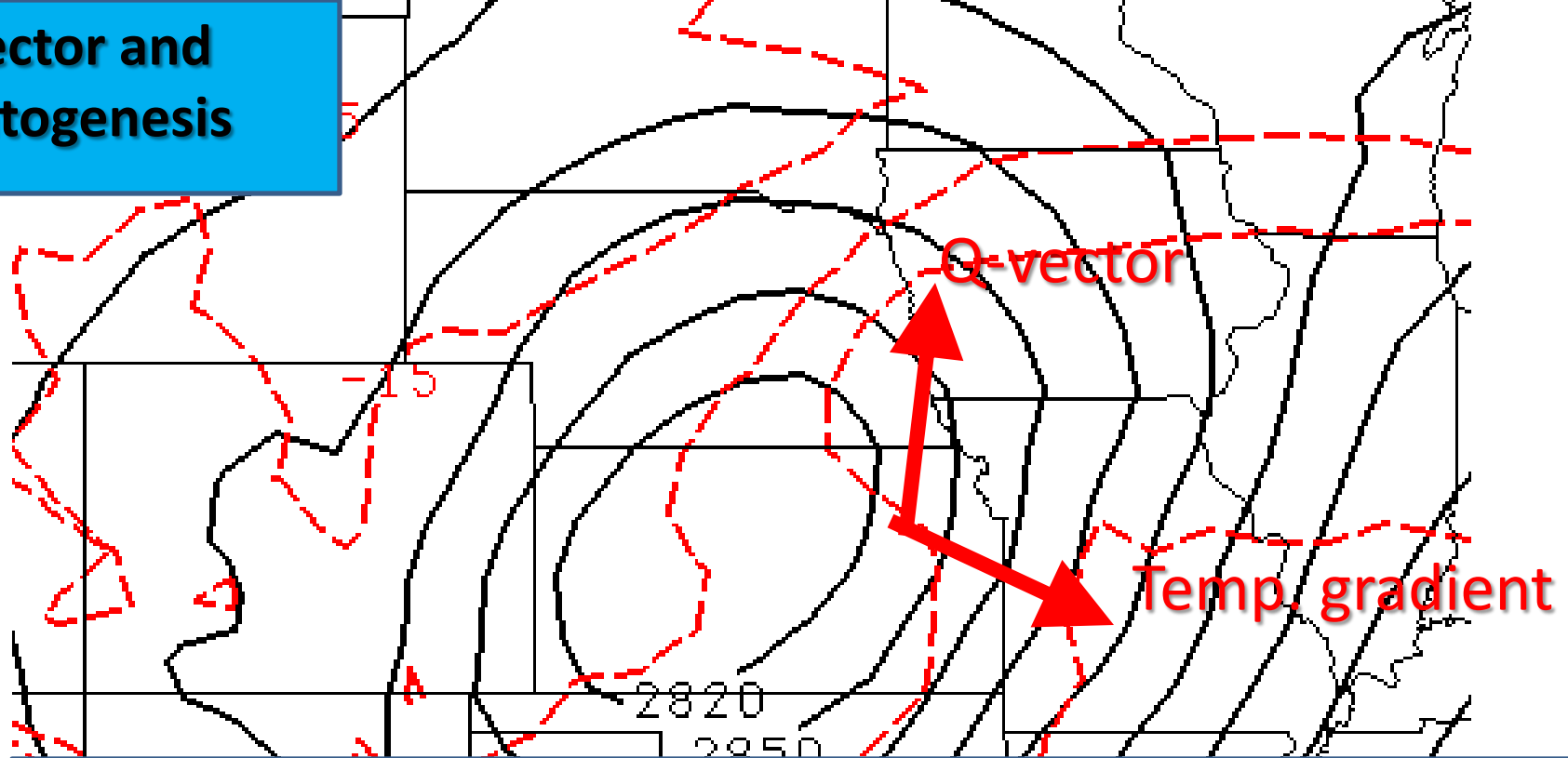
Scaled Q: mult. by  $(1000 \text{ km})^2$

$Q_x = 21 \text{ K m s}^{-1}$

$Q_y = 220 \text{ K m s}^{-1}$

Q vector points nearly due  
(at  $186^{\circ}$  if plot like wind barb)

## Q vector and frontogenesis

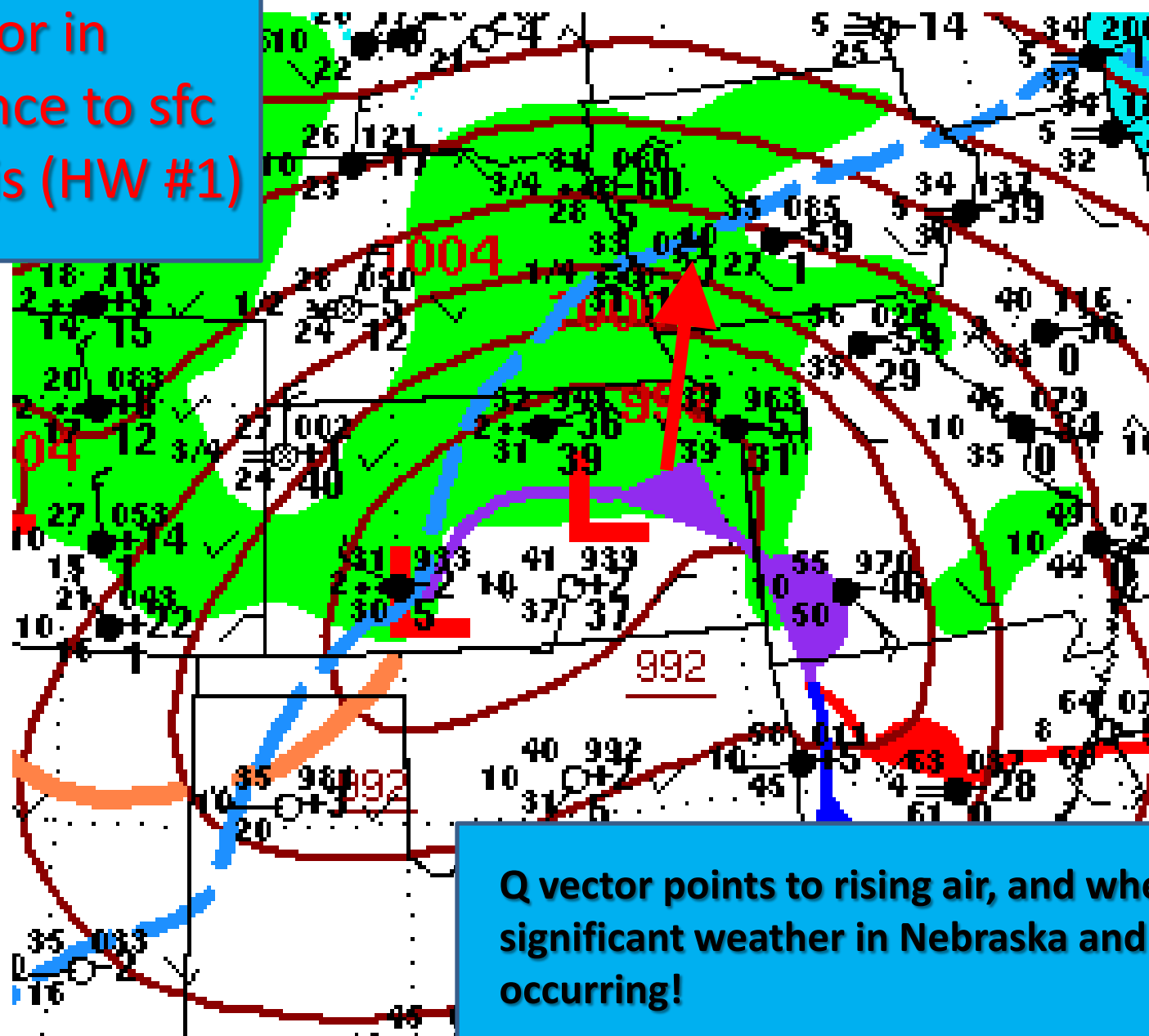


At least at Topeka, the calculated orientation of the Q vector is basically out of phase with the orientation of the temperature gradient in the y direction (from the earlier thermal wind analysis).

Therefore the effect of the geostrophic advection of temperature is frontolytic at this location, tending to weaken the temperature gradient. The compensating ageostrophic circulation is thermally indirect, with cold air rising where it is relatively colder, sinking where warmer.

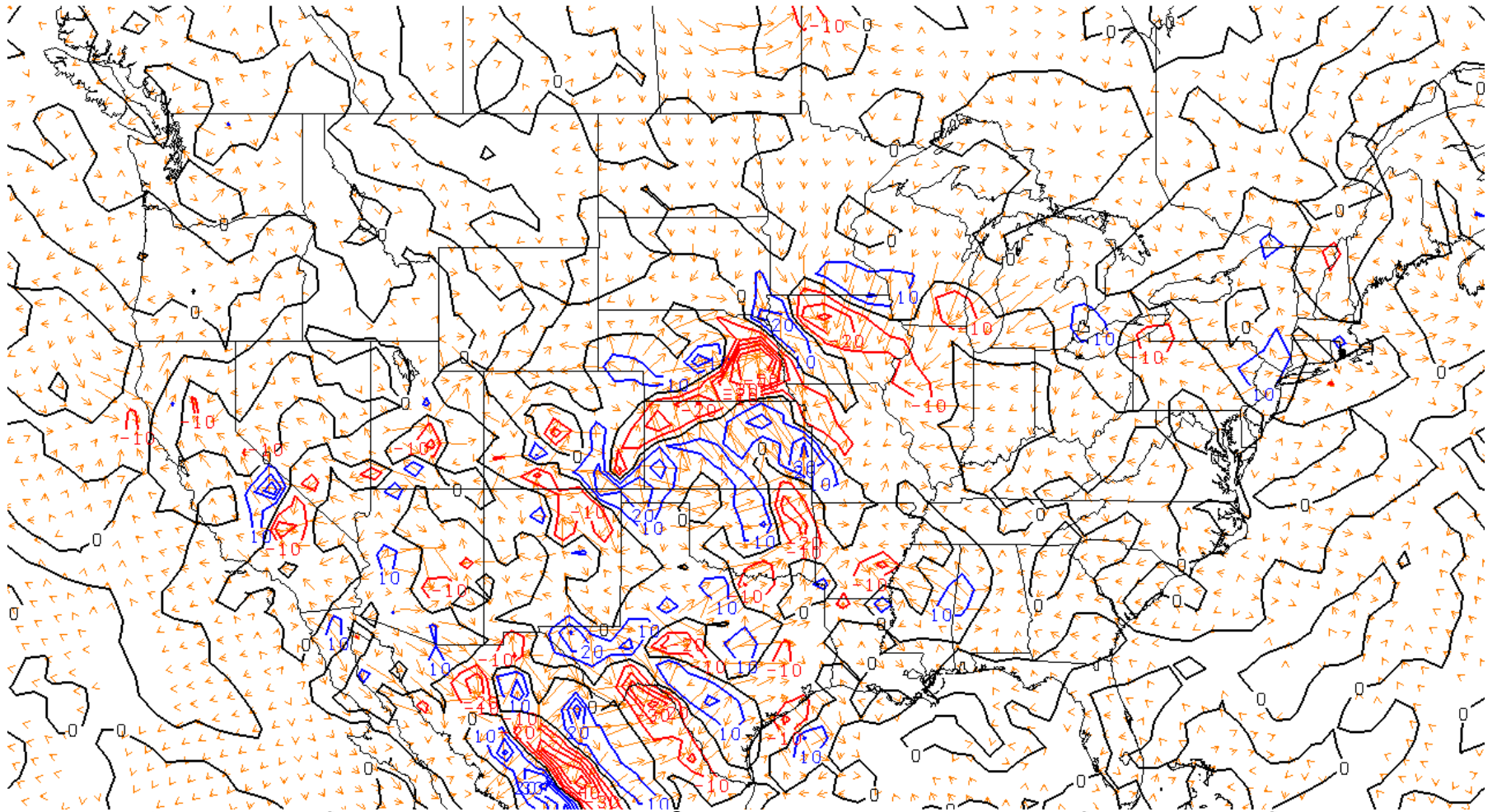


Q-vector in  
reference to sfc  
analysis (HW #1)



Q vector points to rising air, and where most significant weather in Nebraska and Iowa is occurring!

# GEMPAK Q Vector Analysis: Extra credit



**Basic point is that strongest areas of convergence correspond to areas where heaviest precipitation occurring. Needed to additional comment on strengths, weaknesses of Q vectors vs. QG omega for full credit.**

